FPGA Implementation of a Pipelined Kalman Filter for Object Tracking in Two Dimensions

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Abstract—In a location tracking system for a moving object, accuracy and real-time processing are essential factors. The Kalman filter, as a recursive function, stands out as one of the prominent algorithms for object tracking. It continuously compares measured data with predicted values based on the system characteristics in real-time. Then it corrects the error of the predicted values while considering the noise of both system and measured data. This paper focuses on designing a hardware based Kalman filter for object tracking in two dimensions. Following an analysis of the Kalman filter algorithm, the blocks capable of parallel processing are identified and configured to be processed in parallel, effectively reducing data processing time. The clock speed is enhanced by using the pipeline technique. In addition, the time-sharing technique is applied to increase the utilization of hardware resources and reduce the area. Data was processed at 32-bit floating points to uphold accuracy comparable to software-implemented Kalman filters. The proposed Kalman filter architecture is designed using Verilog HDL and then simulated in Synopsys VCS/Verdi. The accuracy is verified by comparing results with a software based Kalman filter designed using MATLAB. It was implemented using Zynq ZYNQ-7 ZC702 Programmable logic via Xilnix Vivado and can operate at 33MHz. It takes 44 clocks, or 1.32 us, to process one data. Therefore, it was confirmed that the designed Kalman filter hardware is suitable for real-time processing.

Keywords—Kalman filter; object tracking; FPGA; parallel processing; pipeline.

I. INTRODUCTION

Research on moving object tracking has been actively conducted in various engineering fields, such as autonomous vehicles, robot control, communication systems, and navigation [1]–[4]. Measurement data is crucial for estimating an object's location, but it often contains significant noise both within and outside the system. The noise diminishes the accuracy of prediction and estimation. Consequently, several algorithms are under investigation to address this challenge, and the Kalman filter is a representative algorithm [5]–[7].

The Kalman filter is a recursive algorithm [8]–[10]. It distinguishes itself from typical filters by dynamically updating its filter coefficients, Kalman gain, over time [11]. It compares noisy measured data with predicted values based on system characteristics. Then, it corrects the predicted value using the prediction error and Kalman gain. It provides estimated values with noise effectively removed, responds in real-time to system state changes, and performs highly efficient calculations [8]–[11].

The Kalman filter is a model for linear systems. Since many systems are nonlinear systems, their application is limited. So, the extended Kalman filter (EKF) has been studied to model nonlinear systems [12]–[14]. Unlike the traditional Kalman filter, the EKF employs a nonlinear mathematical model for the system. It dynamically calculates and applies a linear model based on the previous estimate rather than a predetermined linearization model. Although the EKF is more complex than linear systems, it maintains the fundamental algorithmic principles of the Kalman filter [15], [16].

For more accurate tracking, advanced EKF algorithms integrating various sensors have been studied [17], [18]. Object tracking using artificial intelligence has recently been conducted [19]–[21]. They offer enhanced precision, but their complexity necessitates hardware implementation for real-time processing [22]–[24]. FPGA hardware implementation is facilitated within SoC programmable devices like Xilinx Zynq [25], [26]. This approach reduces communication overhead with software and enhances the efficiency of resource allocation between software and hardware [27]–[29].
In this paper, we design a Kalman filter hardware that estimates an object’s position in two-dimensional space. In FPGA design, we focused on increasing overall resource efficiency through the utilization of pipeline and parallel processing techniques. In the next Section, we introduce the Kalman filter algorithm, and the system model and parameters used. Then, the proposed hardware structure is explained in detail. Section III presents the results of hardware implementation. Finally, conclusions are drawn in Section IV.

II. MATERIALS AND METHOD

A. Kalman Filter Algorithm

The Kalman filter algorithm comprises three main processes, as shown in Fig. 1: a prediction process, a Kalman filter gain calculation process, and an estimation (or update) process [30], [31].

![Kalman Filter Algorithm Diagram](image-url)

The prediction process involves predicting the state x of a system and its error covariance P. These are expressed through the following equations:

\[
\hat{x}_k = A\hat{x}_{k-1} \quad (1)
\]

\[
P_k^- = AP_{k-1}A^T + Q \quad (2)
\]

where the superscripts "-" and "^" mean the predicted value and the estimated value, respectively. The subscript "k" indicates the kth step. If k represents the current state, (k-1) signifies the previous state, and (k+1) signifies the next state. Prediction of the estimate of the current state x is derived from the estimate of the previous state and the system model A. System model A describes how a system changes over time. Therefore, A is a predetermined constant prior to the Kalman filter computation, and it is important to reflect the characteristics of the actual system mathematically accurately.

The process of predicting the error covariance P requires to consider system process noise Q, in addition to the previous error covariance and system model A. Similar to the system model A, system process noise Q is predetermined by the system prior to Kalman filter calculation. As noise arises from various factors, it must be treated as a design variable of the Kalman filter, and an appropriate value must be determined through a trial-and-error process. Noise is typically expressed in statistical terms. The Kalman filter assumes that noise adheres to a standard normal distribution with a mean of 0. Therefore, only the values. Like system process noise Q, it is assumed to follow a normal distribution with a mean of 0. Therefore, only the measurement noise variance requires identification, and its value must be determined through iterative experimentation.

If the measurement noise R is large, the Kalman gain decreases. Consequently, in the correction of the system state outlined in Equation (4), the influence of the measurements decreases, resulting in a more gradual adjustment of the state estimate. Conversely, as the R decreases, the Kalman gain increases, increasing the impact of the measurements.

If the system noise Q is large, the error covariance P becomes large according to Equation (2). As the error covariance P increases, the term in the numerator of the Kalman gain becomes relatively larger compared to the denominator, so the Kalman gain increases. Consequently, during the correction of the system state, the influence of the measurements increases. If the error covariance P is small, the Kalman gain decreases, and the influence of the measurements decreases during the correction of the system state.

B. Mathematical Model for Object Tracking

To track an object moving in a two-dimensional plane, both the position and velocity along the horizontal and vertical axes are considered as the system state. Consequently, the system state x becomes a 4×1 matrix, as shown in the following equation

\[
x = [p_x \ v_x \ p_y \ v_y]^T \quad (6)
\]

where the subscripts "x" and "y" represent the horizontal and vertical axes, respectively, and p and v indicate position and velocity, respectively. The relationship between position and velocity is established as follows,

\[
p_k = p_{k-1} + v_{k-1} \times \Delta t \quad (7)
\]

Assuming that the speed is constant, the system model A is set as follows

\[
A = \begin{bmatrix}
1 & \Delta t & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & 0 & 1 & \Delta t \\
0 & 0 & 0 & 1
\end{bmatrix} \quad (8)
\]

where Δt represents the time interval between position measurements. In this paper, a time interval Δt is set at 1.

Since the measurements are the positions along the horizontal and vertical axes, the matrix H, which represents the relationship between the measured values and the state variables, is configured as a 2×4 matrix as follows.
Since both the system noise $Q$ and the measurement noise $R$ are both assumed to follow a normal distribution with a mean of 0, they are represented as diagonal matrices of $4 \times 4$ and $2 \times 2$, respectively, as follows.

$$Q = \begin{bmatrix} \sigma_{q_{11}}^2 & 0 & 0 & 0 \\ 0 & \sigma_{q_{22}}^2 & 0 & 0 \\ 0 & 0 & \sigma_{q_{33}}^2 & 0 \\ 0 & 0 & 0 & \sigma_{q_{44}}^2 \end{bmatrix} \quad (10)$$

$$R = \begin{bmatrix} \sigma_{r_{11}}^2 \\ 0 \\ 0 \\ \sigma_{r_{22}}^2 \end{bmatrix} \quad (11)$$

Mathworks’ MATLAB is used to verify the algorithm. As verification data, coordinate values of a person’s face in a 2D image are used. System models $A$, $H$, $Q$, and $R$ must be predetermined before the Kalman filter calculation. On the contrary, the state $x$ and error covariance $P$ are recursively updated in real-time, so the initial values must be specified. In this paper, the initial values of $x$ and $P$ were set as follows.

$$x = [0 \ 0 \ 0 \ 0]^T \quad (12)$$

$$P = \begin{bmatrix} 100 & 0 & 0 & 0 \\ 0 & 100 & 0 & 0 \\ 0 & 0 & 100 & 0 \\ 0 & 0 & 0 & 100 \end{bmatrix} \quad (13)$$

Based on repeated simulations, the covariances of $Q$ and $R$ are determined to be 1 and 50, respectively. Consequently, the following matrices are formulated.

$$Q = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad (14)$$

$$R = \begin{bmatrix} 50 \\ 0 \end{bmatrix} \quad (15)$$

By scrutinizing the simulation values for each step, the crucial decision regarding bit precision is made for hardware implementation. Due to the broad range of values involved, performing calculations with a 32-bit floating-point format rather than a 32-bit fixed-point format could enhance accuracy despite the increased hardware complexity.

### C. Algorithm Analysis for Hardware Structure

In this paper, a hardware structure of the Kalman filter is devised to facilitate parallel processing, minimize latency, and optimize area by reusing hardware components. In the prediction process, a matrix multiplier is employed to compute the product of the $4 \times 4$ matrix $A$ and the $4 \times 1$ matrix $x$ to predict the state $x$. Additionally, for covariance prediction, a matrix multiplier and a matrix adder are utilized to process a $4 \times 4$ matrix and a $4 \times 1$ matrix. To predict covariance, matrix multiplication needs to be performed twice, which is executed sequentially. Specifically, using a single matrix multiplier, $AP_{k-1}$ is calculated in the initial step, followed by the calculation of $A^TP_{k-1}A^T$ in the subsequent step.

Since addition typically requires less processing time than multiplication, multiplication and addition operations are combined within a single step. Consequently, a total of two steps are necessary to predict covariance. When calculating the two predicted values, $x$ and $P$, there is no dependence between them. Consequently, the prediction for $x$ and $P$ can be executed in parallel. As a result, a total of two matrix multipliers and one matrix adder are required for the prediction process, which takes two steps.

Fig. 2 shows the essential hardware components and the steps during which each component is utilized. The $matrix\_mul\_1$ and $matrix\_mul\_2$ are matrix multipliers for a $4 \times 4$ matrix multiplied by a $4 \times 1$ matrix and for a $4 \times 4$ matrix multiplied by a $4 \times 4$ matrix, respectively. The $matrix\_add\_1$ is a matrix adder for two $4 \times 4$ matrices. In the prediction process, the $matrix\_mul\_1$ is used during the first step to compute $A\hat{x}_{k-1}$, and the $matrix\_mul\_2$ is used during two steps to compute $AP_{k-1}A^T$. The $matrix\_add\_1$ operates during the second step to compute $P_k$. This parallel processing reduces latency in the Kalman filter prediction process.

![Fig. 2 Essential hardware components and their time schedule](image-url)

To calculate $P_k^T$ included in the Kalman gain, a matrix multiplier for a $4 \times 4$ matrix multiplied by a $4 \times 2$ matrix. However, since $H$ is a constant matrix and only two of its eight elements are the non-zero value, $P_k^TH^T$ can be determined solely through positional transformation without any arithmetic operation as follows.
Performing matrix multiplication using the `matrx_mul_2` for prediction process, in the estimation process, there is no matrix. These two positional transformations result in a 2x2 through a positional transformation as the following equation must be calculated. Since the 2x2 matrix adder is a subset of a 4x4 matrix adder, the and connected seamlessly. A 2x2 matrix adder is required to hardware logic. When connecting the calculation result to the required. The calculation of the Kalman gain is completed byThen, each element of the matrix is divided by the included in the `matrix_mul_2` calculates the determinant. Matrix multiplier includes several multipliers, one multiplier and connected seamlessly. A 2x2 matrix adder is required to hardware logic. When connecting the calculation result to the required. The calculation of the Kalman gain is completed by

\[
P_{k}^{-1} = \begin{bmatrix} P_{k,11} & P_{k,12} & P_{k,13} & P_{k,14} \\ P_{k,21} & P_{k,22} & P_{k,23} & P_{k,24} \\ P_{k,31} & P_{k,32} & P_{k,33} & P_{k,34} \\ P_{k,41} & P_{k,42} & P_{k,43} & P_{k,44} \end{bmatrix}
\]

(16)

Similarly, the calculation of \(HP_{k}^{-1}H^{T}\) can also be achieved through a positional transformation as the following equation (17). These two positional transformations result in a 2x2 matrix.

\[
H P_{k}^{-1} H^{T} = \begin{bmatrix} P_{k,11}^{-1} & P_{k,13}^{-1} \\ P_{k,31}^{-1} & P_{k,33}^{-1} \end{bmatrix}
\]

(17)

Positional transformation does not require separate hardware logic. When connecting the calculation result to the input of other logic, the position of elements can be converted and connected seamlessly. A 2x2 matrix adder is required to add a 2x2 matrix R to the calculation result. Since a 2x2 matrix adder is a subset of a 4x4 matrix adder, the matrix add_1 is used.

To find the inverse of a 2x2 matrix, the determinant \([M]^{-1}\) must be calculated. Since the 2x2 matrix \((HP_{k}^{-1}H^{T} + R)\) is a diagonal matrix according to equations (13), (15), and (17), its determinant calculation requires one multiplier. Since a matrix multiplier includes several multipliers, one multiplier included in the matrix_mul_2 calculates the determinant. Then, each element of the matrix is divided by the determinant. As the matrix is diagonal, two dividers are required. The calculation of the Kalman gain is completed by performing matrix multiplication using the matrix_mul_2 for \(P_{k}^{-1}H^{T}\) and \((HP_{k}^{-1}H^{T} + R)^{-1}\).

In the Kalman gain calculation process, two dividers are added. In one step, \(P_{k}^{H}H^{T}\), \((HP_{k}^{-1}H^{T} + R)\) and the determinants are calculated. Subsequently, division and matrix multiplication are performed in two separate steps. Therefore, a total of three steps are needed. Like in the prediction process, in the estimation process, there is no dependency between state and error covariance, both can be executed in parallel. To estimate covariance, matrix multiplication of the 4x2 matrix Kalman gain and 2x4 matrix H is required. This is accomplished using the matrix_mul_2. Simultaneously, for state update, matrix multiplication of the 4x2 matrix Kalman gain and 2x1 matrix z is calculated using the matrix_mul_1. The reason why \(Hx_{k}^{-}\) is not calculated first is that it cannot be calculated with the matrix_mul_1. Unless a matrix multiplier is newly added, the covariance and state cannot be calculated simultaneously. In the second step of the covariance estimation, \(K_{k}Hx_{k}^{-}\) is calculated using the matrix_mul_2, followed by subtraction from P using the matrix add_1. To estimate the state, \(K_{k}H\) calculated in the previous step is multiplied by \(x_{k}^{-}\) using the matrix_mul_1, followed by two additional 4x1 matrix addition. In the final step of the estimation process, three 4x1 matrix adder with four elements is needed. As shown in Fig. 2, the proposed Kalman filter needs two matrix multipliers, three matrix adders, and two divisors and requires a total of seven steps.

### A. Hardware Structure

The proposed Kalman filter hardware for 2D object tracking consists of two matrix multipliers, three matrix adders, two dividers, some combinational logic and controller shown in Fig. 2. There are measurements z as inputs to the system. The input measurements are converted into an IEEE 754 single precision format, and each operation is processed in a pipeline structure.

1) \([4\times4] \times [4\times4] \text{ Matrix Multiplier}: To multiply a 4x4 matrix A and a 4x4 matrix B, each element in one row of A must be multiplied with each element in one column of B, and the resulting four values must be added to calculate one element of the resulting matrix C. Since C is a 4x4 matrix, this process must be repeated 16 times. In other words, a matrix multiplication of a 4x4 matrix and a 4x4 matrix requires 64 multiplication operations.

The matrix multiplier in the proposed hardware design consists of four multipliers. As shown in Fig. 3, matrix A and matrix B elements are fed into the multiplier, and the resulting element is computed as the sum of the products of corresponding elements of matrix A and matrix B. An element \(C[0][0]\) of a resulting matrix C is \((A[0][0] \times B[0][0]) + (A[0][1] \times B[1][0]) + (A[0][2] \times B[2][0]) + (A[0][3] \times B[3][0])\). Generally, \(C[i][j] = (A[i][0] \times B[0][j]) + (A[i][1] \times B[1][j]) + (A[i][2] \times B[2][j]) + (A[i][3] \times B[3][j])\). Thus, four elements of one row of matrix A are arranged as the same number input port of the four multiplexers, respectively. When sel_mode_A = i, A[i][0], A[i][1], A[i][2], and A[i][3] are selected and used as multiplier inputs, respectively. On the other hand, the four elements of one column of matrix B are arranged as the same number input port of the four multiplexers, respectively. When sel_mode_B = j, B[0][j], B[1][j], B[2][j], and B[3][j] are selected and used as multiplier inputs, respectively. Therefore, eight elements required for \(C[i][j]\) are selected by the signals, sel_mode_A and sel_mode_B. In this case, the sel_mode_B changes its value every cycle clock, iterating through 0→1→2→3 four times, to select elements from different columns of B. The sel_mode_A changes its value every four clock cycles, iterating through 0→1→2→3 once, to select elements from different rows of B. This process computes \(C[0][0], C[0][1], C[0][2], \ldots, C[3][2], C[3][3]\) in order. A total of 16 clock cycles are required.

This matrix multiplier, initially designed for 4x4 matrix multiplication by 4x4 matrix, is also used 4x2 matrix multiplication by 2x2 matrix. In this configuration, a total of 8 elements needs to be calculated for the resulting 4x2 matrix. So, the inputs of the multiplexer and the signals, sel_mode_A and sel_mode_B, must be changed. In Fig. 3, the inputs of the top two multipliers remain unchanged, while the inputs of the bottom two multipliers are modified.
Fig. 3 Block diagram of a 4×4 matrix multiplier by a 4×4 matrix

The inputs of multiplexers that select the elements of matrix A are changed to A[2][0], A[3][0], A[2][1], and A[3][1] instead of A[0][2], A[1][2], A[0][3], and A[1][3], respectively. The multiplexers that select the elements of the matrix B are not used. Instead, the elements of B selected in the upper multiplexers are utilized as multiplier inputs. The sel_mode_B repeats sequentially from 0 to 1 twice every clock cycle, while the sel_mode_A changes from 0 to 1 once every two clock cycles. Therefore, the operation requires a total of 4 clock cycles to compute the resulting 4×2 matrix.

2) 4×4 × 4×1 Matrix Multiplier: Fig. 4 shows a 4×4 matrix multiplier by a 4×1 matrix. In contrast to the 4×4 matrix multiplier by 4×4 matrix, this design does not require a multiplexer for matrix B. That is, only sel_mode_A changes sequentially from 0 to 3 every clock cycle, indicating the row selection from a matrix A. The calculation is completed in a total of 4 clocks. The calculation is completed in a total of 4 clock cycles, as each clock cycle processes one row of the matrix A. The matrix multiplier, originally designed for 4×4 matrix multiplication by 4×1 matrix, is repurposed for 4×2 matrix multiplication by 2×1 matrix. In Fig. 4, the inputs of the top two multipliers remain unchanged. On the other hand, the inputs of the bottom two multipliers are changed. The inputs of multiplexers that select the elements of matrix A are changed to A[20], A[30], A[21], and A[31] instead of A[02], A[12], A[03], and A[13], respectively. The multiplexers that select the elements of the matrix B are not used. Instead, the elements of B selected in the upper multiplexers are utilized as the multiplier inputs. The sel_mode_A changes from 0 to 1 once every clock. Therefore, a total of 2 clocks are required to complete the operation.

Fig. 4 Block diagram of a 4×4 matrix multiplier by a 4×1 matrix

3) Matrix adders: A matrix adder consists of adders between elements in each matrix position. Since the largest matrix of this Kalman filter is 4x4 matrix, at least 16 adders are required to perform matrix addition within one clock cycle. Three matrix additions are calculated in step 7 of the Kalman filter operation. In detail, two 4x1 matrix adders and
one 4x4 matrix adder are required, resulting in 24 adders. In 2 and 3 steps, the 4x4 matrix adder is utilized among them. Furthermore, matrix adders are also utilized as submodules of the matrix multipliers. A 4x4 matrix multiplier by 4x4 matrix and a 4x4 matrix multiplier by 4x1 matrix contains three 4x4 matrix adders and three 4x1 matrix adders, respectively.

4) Floating point multiplier: The matrix multipliers consist of floating-point multipliers. The floating-point multiplier operates by separately calculating the multiplication of mantissas and the addition of exponents. And then, normalization is done to meet single precision standards.

5) Floating point divider: Floating point dividers are needed to calculate the inverse of a matrix. Similar to the floating-point multiplier, the floating-point divider operates by separately handling the division of mantissas and the addition of exponents. And then, normalization is done to meet single precision standards.

6) Floating point adder: Unlike the floating-point multiplier and divider, the mantissas are shifted according to the difference in exponents, added together, and then normalized.

III. RESULTS AND DISCUSSION

The proposed Kalman filter hardware is designed using Verilog HDL and functionally verified using Synopsys' VCS/Verdi. Its simulation results are compared with the software Kalman filter designed in Mathwork’s MATLAB. As test data comprise the human face coordinates extracted from the video using OpenCV and are utilized as measurements to both Kalman filters. As simulation results, the estimated human face coordinates from the designed hardware Kalman filter differ from those of the software Kalman filter in the first decimal place. This difference can be attributed to various factors. While the software Kalman filter uses 64-bit double precision, the hardware Kalman filter uses 32-bit single precision. In addition, the designed hardware uses the clipping method among several rounding techniques. Despite these differences, considering that the object’s coordinates are expressed in integer units, the error in the first decimal place is deemed sufficiently small. Table 1 compares the software and hardware results for the first cycle.

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**TABLE I**

<table>
<thead>
<tr>
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<th>SW Kalman filter</th>
<th>HW Kalman filter</th>
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<tbody>
<tr>
<td>$K_k$</td>
<td>0.8008 0</td>
<td>0.7979 0</td>
</tr>
<tr>
<td></td>
<td>0.3984 0</td>
<td>0.3968 0</td>
</tr>
<tr>
<td></td>
<td>0 0.8008</td>
<td>0 0.7979</td>
</tr>
<tr>
<td></td>
<td>0 0.3984</td>
<td>0 0.3968</td>
</tr>
<tr>
<td>$\hat{x}_k$</td>
<td>497.29 247.45 217.01 107.96</td>
<td>495.35 246.44 216.16 107.54</td>
</tr>
<tr>
<td>$P_k$</td>
<td>40 19 0 0 0</td>
<td>42 21 0 0</td>
</tr>
<tr>
<td></td>
<td>19 61 0 0</td>
<td>21 58 0 0</td>
</tr>
<tr>
<td></td>
<td>0 0 40 19</td>
<td>0 0 42 21</td>
</tr>
<tr>
<td></td>
<td>0 0 19 61</td>
<td>0 0 21 59</td>
</tr>
</tbody>
</table>

The clock period is set to 30 ns. Table 3 shows the design timing summary after the post-fit. These results demonstrate that the designed Kalman filter hardware meets the timing requirements, allowing it to operate at the desired clock frequency of 33.3 MHz. Additionally, it is expected to operate at a maximum clock frequency of 34.2 MHz.

Fig. 5 shows the prediction and estimation value for the coordinates of the human face in the video. It is confirmed that the proposed hardware Kalman filter estimates well the object’s location according to its movement in continuous motion.

Fig. 6 shows the schematic of the top module confirmed by Verdi. After completing functional verification, Xilinx Vivado is used for FPGA implementation using Xilinx ZYNQ-7 ZC702 Evaluation board. Table 2 provides a summary of the number of components, such as slice LUTs table and slice registers, utilized by the design.
processing time of 1.32 us. It was confirmed that the latency of the proposed hardware Kalman filter is approximately 1/1000th of the latency of the software Kalman filter.

The execution time of the software Kalman filter includes system overhead, which may not be directly comparable to the latency of the hardware Kalman filter. Considering that the input data for the hardware Kalman filter is stored in memory, the overhead due to communication with software is minimal. However, even if the CPU time is around 50% of the total execution time for the software Kalman filter, the latency of the software implementation is still approximately 600 us. Consequently, the hardware Kalman filter demonstrates significantly lower processing time than the software implementation. The designed Kalman filter is implemented using the programmable logic of ZYNQ-7 ZC702. If it is implemented in SoC, including processing systems, it is expected to enhance both efficiency and performance, making the Kalman filter more suitable for real-time applications.

IV. CONCLUSION

In this paper, the pipelined Kalman filter for object tracking in two dimensions is implemented in hardware. The hardware implementation offers advantages such as parallel processing and increased resource utilization through pipeline techniques and time sharing. In particular, when the same operation is performed using data of different sizes at different times, the hardware is designed based on the largest data size and selectively used to reduce the hardware area and increase efficiency. It is designed with Verilog HDL and compiled using Synopsys’ VCS/Verdi. Its functionality is verified by comparing its simulation results with the Kalman filter in Mathwork’s MATLAB. It is implemented on an FPGA using ZYNQ-7 ZC702. Approximately 47 k slice LUTs, 64 DSPs, and 12 k slice registers are used. The clock speed is 33MHz, and 44 clock cycles are required to process one data. Therefore, the processing time is 1.32 us. It is confirmed that the proposed hardware Kalman filter is more than 1000 times faster than the software Kalman filter. In the future, we plan to implement it in SoC to enhance its usability further.

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